

DESIGN OF STEEL GRILLAGE FOUNDATION FOR AN AUDITORIUM

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Abstract - Grillage foundation may provide an economical alternative to offshore ‘mud mat’ foundations for seabed infrastructure, owing to their improved hydrodynamic characteristics, which are important during installation. The foundation of the grid structure is a solid steel frame. The lower base is located on a soil layer at the desired level. Offshore loadings on these foundations consist of vertical (dead weight) and horizontal ‘in-service’ loads. However, to date there is no accepted method of design, as foundation capacity may differ significantly from that of conventional solid shallow foundations. This is design of the grillage foundation that is to be constructed at Mannivakam. In our project we are analysing the analytical method of design to calculate the variation of vertical bearing capacity with grill penetration in the sand. The members like beams, columns, grid slab, footing and slab are manually designed using IS 456-2000 code book.

Keywords- grillage foundation, vertical bearing capacity, grid structure, Offshore loadings.

1. INTRODUCTION

1.1 GENERAL

A foundation is the element of an architectural structure which connects it to the ground, and transfers loads from the structure to the ground. Foundations are generally considered either shallow or deep. Foundation engineering is the application of soil mechanics and rock mechanics in the design of foundation elements of structures.

Shallow foundations, often called footings, are usually embedded about a meter or so into soil. One common type is the spread footing which consists of strips or pads of concrete which extend below the frost line and transfer the weight from walls and columns to the soil or bedrock. Another common type of shallow foundation is the slab-on-grade foundation where the weight of the structure is transferred to the soil through a concrete slab placed at the surface. Slab-on-grade foundations can be reinforced mat slabs, which range from 25 cm to several meters thick, depending on the size of the building, or post-tensioned slabs, which are typically at least 20 cm for houses, and thicker for heavier structures.

A deep foundation is used to transfer the load of a structure down through the upper weak layer of topsoil to the stronger layer of subsoil below. There are different

types of deep footings including impact driven piles, drilled shafts, caissons, helical piles, geo-piers and earth stabilized columns. The naming conventions for different types of footings vary between different engineers. Historically, piles were wood, later steel, reinforced concrete, and pre-tensioned concrete.

1.2 GRILLAGE FOUNDATION

Grillage foundation is the most economical foundation in case of transferring heavy loads from columns to soil of low bearing capacity. A type of foundation often used at the base of a column. It consists of one, two or more tiers of steel beams superimposed on a layer of concrete, adjacent tiers being placed at right angles to each other, while all tiers are encased in concrete.

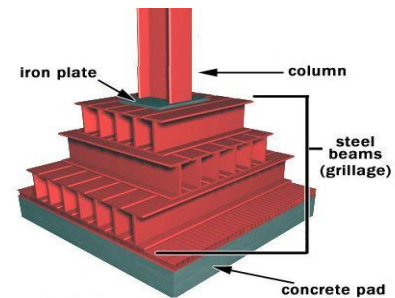


Fig. 1: Typical Layout of Grillage Foundation

2. Plan

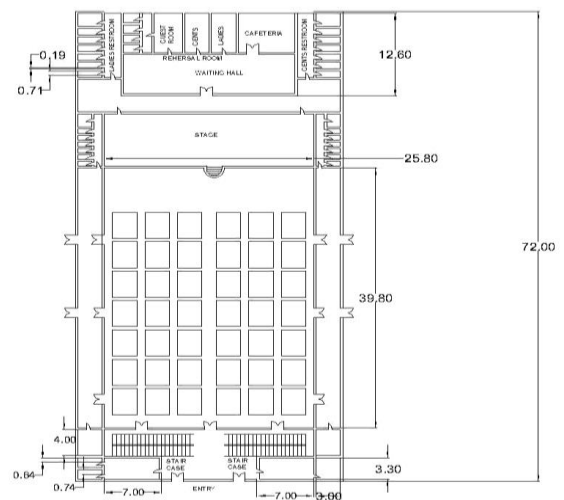


Fig 2: Plan for Auditorium

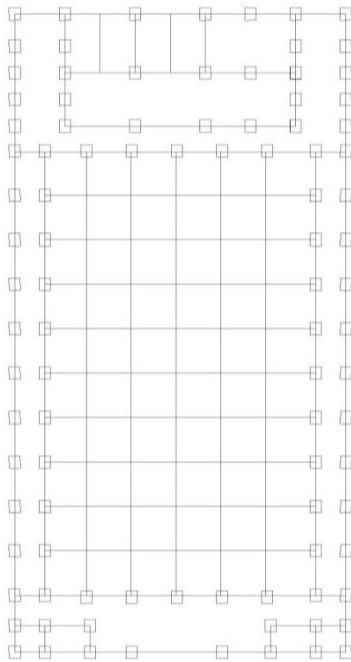


Fig. 3: Grid Slab Layout

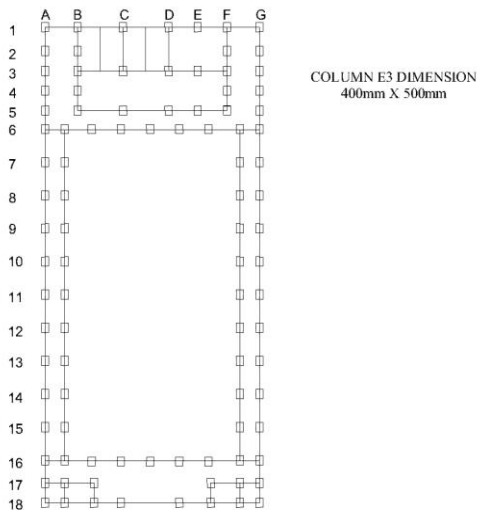


Fig. 4: Column Layout

3. DESIGN OF SLAB

Data:

- L_x = 3 m Shorter span
 - L_y = 5 m Longer span
 - F_{ck} = 30 N/mm²
 - F_y = 415 N/mm²
 - Live load = 4kN/ m²
 - Floor finish = 1 kN/ m²
 - L_x / L_y = 1.67 < 2
- So, the slab must be designed by two way slab.

Step 1: Thickness of slab

$$\begin{aligned} \text{Effective depth } d &= 107.142 \\ &= 110 \text{ mm (approx.)} \\ \text{Overall depth } D &= 110 + 5 + 20 \text{ (cover)} \\ &= 135 \text{ mm} \end{aligned}$$

Step 2: Effective span

$$L = 3 + 0.110 = 3.11 \text{ m}$$

Step 3: Load calculation

Consider 1m length of the slab.

Self weight of the slab = 3.375 kN/m

Live load = 4 kN/m

Floor finish = 1 kN/m

Total load = 8.375 kN/m

Factored load = 12.5625 kN/m

Step 4: Design moment and SF

$$\begin{aligned} M_x &= \alpha_x W_u L^2 \\ L_x / L_y &= 1.67, \\ \alpha_x &= 0.046 \\ \alpha_y &= 0.028 \\ M &= 5.58 \text{ kN.m} \\ M_y &= 3.402 \text{ kN.m} \\ V_u &= 0.5 W_u \\ &= 19.53 \text{ kN} \end{aligned}$$

Step 5: Check for effective depth

$$\begin{aligned} d &= \sqrt{\frac{M_x}{0.138 F_{ck} b}} = \sqrt{\frac{5.58 \cdot 10^6}{0.138 \cdot 30 \cdot 1000}} \\ &= 36.712 \\ &= 40 \text{ mm (approx.)} \end{aligned}$$

$d_{\text{required}} < d_{\text{provided}}$
Hence, safe

Step 6: Main reinforcement for shear span

$$\begin{aligned} M_{ux} &= 0.87 F_y A_{st} d \left[1 - \frac{F_y A_{st}}{F_{ck} b d} \right] \\ A_{st} &= 143.073 \text{ mm}^2 \\ \text{Using 10 mm } \phi \text{ of bars,} \\ \text{No. of bars} &= 1.82 = 2 \text{ bars} \\ A_{st} \text{ provided} &= 157.07 \text{ mm}^2 \\ \text{Spacing of bars} &= 500 \text{ mm} \\ \text{Not possible, adopt 300 mm} \\ \text{So, provide 2 no's of 10 mm } \phi \text{ bars @ 300 mm c/c} \\ 1. \text{ Width of middle strip} &= \frac{3}{4} L_y \\ &= 3.8325 \text{ m} \\ 2. \text{ Width of edge strip} &= \frac{1}{8} L_y \\ &= 0.638 \text{ m} \end{aligned}$$

Step 7: Main reinforcement for longer span

$$M_{uy} = 0.87 F_y A_{st} d \left[1 - \frac{F_y A_{st}}{F_{ck} b d} \right]$$

$$A_{st} = 86.602 \text{ mm}^2$$

$$\text{No. of bars} = 3 \text{ bars}$$

$$A_{st} \text{ provided} = 78.53 \text{ mm}^2$$

$$\text{Spacing of bars} = 345.12 \text{ mm}$$

Not possible, adopt 300 mm
 So, provide 3 no of 10 mm ϕ bars @ 300 mm c/c

1. Width of middle strip = $\frac{3}{4} L_x$
 = 2.332 m
2. Width of edge strip = $\frac{1}{8} L_y$
 = 0.388 m

Step 8: Distribution, reinforcement

$$A_{st} = 0.12 \times b \times D$$

$$= 162 \text{ mm}^2$$

Using 8 mm ϕ of bars
 No. of bars = 3.22 = 4 bars
 Spacing of bars = 300 mm (approx.)
 So, provide 4 no's of 10 mm ϕ bars @ 300 mm c/c

Step 9: Torsional reinforcement

Size of the torsional length = $L_x/5$
 = 0.62 m

Area of torsional reinforcement = $\frac{3}{4} A_{st}$
 = 117.8 mm²

Using 10 mm ϕ of bars,
 No. of bars = 2.49 = 3 bars
 A_{st} provided = 157.07 mm²
 Spacing of bars = 355 mm
 Not possible, adopt 300 mm
 So, provide 3 no's of 10 mm ϕ bars @ 300 mm c/c

Step 10: Check for shear

$$\tau_v = 0.177 \text{ N/mm}^2$$

$$P_t = 0.142$$

$$\tau_c = 0.36 \text{ N/mm}^2$$

$\tau_v < \tau_c$, The slab is safe in shear

Step 11: Check for deflection

$$(L/d)_{\text{provided}} < (L/d)_{\text{max}}$$

$$(L/d)_{\text{provided}} = 28.27$$

$$(L/d)_{\text{max}} = (L/d)_{\text{basic}} \times K_t \times K_f \times K_c$$

$$P_t = 0.142$$

$$K_t = 1.55$$

Hence safe

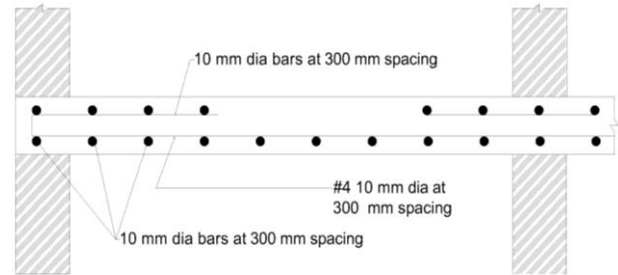


Fig 5: Reinforcement Details of Slab Section

3.2 GRID SLAB DESIGN

Grid size	=	51m x 27m
Spacing of ribs	=	3m c/c
Concrete	=	M30 grade
Steel	=	Fe415

DIMENSIONS OF SLABS AND BEAMS

Thickness of slab	=	300mm
Depth of ribs based on span/depth	=	$27 \times 10^3 / 20$
	=	1250mm \approx 1300mm
Assume width of rib	=	500mm
Adopt overall depth of ribs	=	1000mm

LOADS

Wt. of slab	=	0.1 x 25
	=	2.5 kN/m ²
Total load of slab	=	2.5 x 27 x 51
	=	3304.8 kN
Wt. of ribs	=	12.5kN/m
Total wt. of beams (x-direction)	=	17 x 12.5 x 27
	=	5737.5kN
Total wt. of beams (y-direction)	=	9 x 12.5 x 51
	=	5737.5 kN
Total wt. of FF	=	0.6 x 27 x 51
	=	826.2kN
Total live load	=	3 x 27 x 51
	=	4131 kN
Total live load and dead load on grid floor	=	19737 kN
Load per m ²	=	19737 / (27 x 51)
	=	14.33 kN/m ²
Ultimate load per m ²	=	14.33 x 1.5
	=	21.49 kN/m ²

APPROXIMATE METHOD (MOMENTS)

If q_1 and q_2 are the loads shared in the x & y direction

$$\begin{aligned}
 q_1 &= q (b_y^4 / (a_x^4 + b_y^4)) \\
 &= 21.48(51^4 / (27^4 + 51^4)) \\
 &= 19.92 \text{ kN/m} \\
 q_2 &= q (a_x^4 / (a_x^4 + b_y^4)) \\
 &= 21.48(27^4 / (27^4 + 51^4)) \\
 &= 1.564 \text{ kN/m}
 \end{aligned}$$

Moments in x & y direction at center of grid or 2m width

$$\begin{aligned}
 M_x &= (q_1 \times b_1 \times a^2 / 8) \\
 &= (19.92 \times 3 \times 27^2 / 8) \\
 &= 5445.63 \text{ kN.m} \\
 M_y &= (q_2 \times a_1 \times b^2 / 8) \\
 &= (1.564 \times 3 \times 51^2 / 8) \\
 &= 1525.48 \text{ kN.m}
 \end{aligned}$$

SHEAR FORCE CALCULATIONS

Shear force in beams running in x direction

$$\begin{aligned}
 Q_x &= q_1 a b_1 / 2 \\
 &= 18.82 \times 3 \times 27 / 2 \\
 &= 806.76 \text{ kN}
 \end{aligned}$$

Shear force in beams running in y direction

$$\begin{aligned}
 Q_y &= q_2 b a_1 / 2 \\
 &= 1.564 \times 3 \times 51 \\
 &= 119.64 \text{ kN}
 \end{aligned}$$

RIGOROUS METHOD (Plate theory)

Section properties:

$$\begin{aligned}
 D_f / D &= 300 / 1300 \\
 &= 0.23 \\
 b_w / b_f &= 500 / 3000 \\
 &= 0.167
 \end{aligned}$$

Second moment of inertia of beam in x direction and in y direction (I_2)

$$I = C \cdot b \cdot w \cdot D^3$$

Where,

$$\begin{aligned}
 C &= \text{constant } (C=0.19) \\
 &= 0.19 \times 500 \times 1300^3 \\
 &= 2.10 \times 10^{11} \text{ mm}^4
 \end{aligned}$$

If I_1 & I_2 are the second moment of area of tee-section about their centroidal axis in the x and y direction respectively.

$$\text{So } I_1 = I_2 = I$$

$$\begin{aligned}
 \text{And } a_1 = b_1 &= 3m \\
 &= 3 \times 10^{12} \text{ mm}^4
 \end{aligned}$$

Flexural rigidity per unit length of plate along x direction

$$\begin{aligned}
 D_x &= EI_1 / b_1 \\
 &= E \times 2.08 \times 10^{11} / 3 \times 10^{12}
 \end{aligned}$$

$$D_x \& D_y = 0.06933E$$

The torsional rigidity in the x and y directions are

$$\begin{aligned}
 c_1 = c_2 &= k_1 G (2a)^3 2b \\
 G &= E / 2(1 + \mu) \quad (\mu=0.15) \\
 &= 0.43478E \\
 k_1 &= \text{constant of torsional rigidity by Timoshenko} \\
 k_1 = k_2 &= 0.263 \\
 C_1 = C_2 &= 1.42 \times 10^{10} \text{ Emm}^4 \\
 &= 0.0142E \\
 E &= 5700 \times (30)^{1/2} \\
 E &= 31.22 \times 10^6 \text{ kN/m}^2
 \end{aligned}$$

DEFLECTION AT CENTRE SPAN

$$\begin{aligned}
 (D_x / a_x^4) &= 0.06933E / 27^4 \\
 &= 0.06933 \times 31.22 \times 10^6 / 27^4 \\
 (D_x / a_x^4) &= 2.073 \\
 (D_y / b_y^4) &= 0.06933 \times 31.22 \times 10^6 / 51^4 \\
 &= 0.3199 \\
 (2H / a_x^2 b_y^2) & \\
 \text{Where, } 2H &= c_1 / b_1 + c_2 / a_1 \\
 &= 0.43478E / 3 + 0.43478E / 3 \\
 &= 0.0948E \\
 (2H / a_x^2 b_y^2) &= 0.0948 \times 31.22 \times 10^6 / (27^2 \times 51^2) \\
 &= 0.156
 \end{aligned}$$

The deflection at centres of plate is given by the equation

$$A = 0.0724$$

The modified modulus of elasticity

$$E_{ce} = E_c / (1 + \theta)$$

Creep co-efficient

$$\theta = 0.4$$

$$= E_c / 1.4$$

Long term deflection

$$= 1.4 \times 0.0724$$

$$= 0.10136$$

According to IS 456:2000 the long term deflection should not exceed

$$\text{Span} / 250 = 27 / 250$$

$$= 0.108m$$

$$\text{So } 0.108 > 0.10136$$

The maximum deflection including long term effects lies within the permissible limits.

DESIGN OF MOMENTS

The bending moments, torsional moments and stress at various points are computed the equation.

$$\begin{aligned}
 M_x &= D_x (\sigma^2 a / \sigma_x^2) \\
 M_x &= 2121.61 \{ (\sin(x\pi/a) \times (\sin(y\pi/b))) \\
 M_y &= D_y (\sigma^2 a / \sigma_y^2) \\
 &= 594.63 \text{ kN.m} \{ (\sin(x\pi/a) \times (\sin(y\pi/b))) \\
 M_{xy} &= -(c_1 / b_1) (\sigma^2 a / \sigma_x \sigma_y) \\
 &= -76.62 \{ (\cos(x\pi/a) \times (\cos(y\pi/b))) \\
 M_{xy} &= -(c_2 / a_1) (\sigma^2 a / \sigma_x \sigma_y) \\
 &= -76.62 \{ (\cos(x\pi/a) \times (\cos(y\pi/b)))
 \end{aligned}$$

DESIGN OF SHEAR

$$\begin{aligned} \theta_x &= \sigma/\sigma_x(D_x (\sigma_u^2/\sigma_x^2) + (c_2/a_1) (\sigma^2 a/\sigma_y^2)) \\ \theta_x &= -251.25((\cos(x\pi/a) \times (\cos(y\pi/b))) \\ \theta_y &= \sigma/\sigma_y(D_y (\sigma_u^2/\sigma_y^2) + (c_1/b_1) (\sigma^2 a/\sigma_x^2)) \\ &= -45.55((\sin(x\pi/a) \times (\cos(y\pi/b))) \end{aligned}$$

TABLE 1: Maximum Shear Force In Grid Slab

METHOD	Q _x	Q _y
Approximate method (ranking grash off theory)	806.76 kN	119.64 kN
Rigorous analysis (plate theory)	251.58 kN	45.55 kN

TABLE 2: Maximum Moments In Grid Slab

METHOD	M _x	M _y
Approximate method (ranking grash off theory)	5445.63 kN.m	1525.48 kN.m
Rigorous analysis (plate theory)	2121.61kN.m	594.63kN.m

DESIGN OF REINFORCEMENTS

Maximum ultimate working moment
 $M_u = 5445.63 \text{KN.m}$
 Moment capacity of flange section
 $M_{uf} = 0.36f_{ck}b_f D_f (d - 0.42D_f)$
 $D = D - d'$
 $= 09 \times 10^{10} \text{N.mm}$
 $= 10925.98 \text{kN.m}$

Since $M_u < M_{uf}$

Neutral axis falls within the flange
 $M_u = 0.87f_y A_{st} d (1 - (A_{st} f_y / f_{ck} b d))$
 $A_{st} = 12659.58 \text{mm}^2$

Provide 26 bars of 25mm dia bars
 $A_{stpr} = 12762.62 \text{mm}^2$
 Spacing = 35mm c/c

Maximum ultimate shear force
 $V_u = 806.76$
 $\tau_v = v_u / b d$
 $= 0.125 \text{N/mm}^2$

Assuming 13 bars to be bent up near the supports

A_{st} at supports = 6381.31 mm²
 $(100 A_{st} / b d) = 100 \times 6381.31 / 3000 \times 1250$
 $= 0.17$

From IS 456:2000 (pg. no: 73)
 $\tau_c = 0.306 \text{N/mm}^2$

Since $\tau_c < \tau_v$

Hence safe

So minimum shear reinforcements shall be provided (IS 456:2000 (pg. no: 72)

$S_v = 0.87 A_{sv} F_y / 0.4b$
 $= 121.98 \text{mm}$

Provide 16mm dia bars of two legged stirrups at 130mm c/c at supports and the spacing gradually increased to 200mm towards the center of span.

Maximum ultimate moment in central rib in y-direction

$M_u = 1525.48 \text{kN.m}$
 $M_u = 0.87 f_y A_{st} d (1 - (A_{st} f_y / f_{ck} b d))$
 $A_{st} = 3423.56 \text{mm}^2$

Provide 18 bars of 16mm dia

$A_{stpr} = 3619.08 \text{mm}^2$
 Spacing = 55.56mm c/c = 50 mm

4.3 DESIGN OF BEAM

M-30 grade of concrete

Fe-415 grade of steel

Width of support = 230mm

Span = 6000mm

DIMENSION OF BEAM

Provide 230mm width

$D = L/10$
 $D = 6000/10$
 $= 600 \text{mm}$
 Effective cover = 25mm
 $D = 600 - 25$
 $d = 575 \text{mm}$

EFFECTIVE SPAN

Clear span + width of the support

$6 + 0.23 \text{m} = 6.23 \text{m}$

Clear span + effective depth

$4 + 0.575 = 4.575 \text{m}$

LOAD CALCULATION

Self-weight of beam

$= 25 \times 0.23 \times 0.6$
 $= 3.45 \text{KN/m}$

Load from slab = 12.525KN/m

Load from brick wall

$= 0.23 \times 3 \times 20.5$

$= 14.145 \text{KN/m}$

Total UDL (W) = $(3.45 + 14.145) \times 1.5$

$= 26.39 \text{KN/m}$

Design load = UDL + slab load

$= 26.39 + 12.525$

$= 38.92 \text{KN/m}$

MOMENT AND SHEAR FORCE

$$\begin{aligned}
 M_u &= wl^2/8 \\
 &= 38.92 \times 6^2/8 \\
 &= 175.12\text{kN/m} \\
 V_u &= WL/2 \\
 &= 38.92 \times 6/2 \\
 &= 116.67\text{kN} \\
 M_{u\text{lim}} &= 0.138 f_{ck} b d^2 \\
 &= 0.138 \times 30 \times 230 \times 575^2 \\
 &= 314.82\text{kNm} \\
 M_u < M_{u\text{lim}} &\text{ section is under reinforced} \\
 A_{st} &= 934.96\text{mm}^2 \\
 \text{Provide 16mm bar} \\
 \text{No of bars} &= 5 \text{ bars}
 \end{aligned}$$

SHEAR REINFORCEMENT

$$\begin{aligned}
 a_{st\text{min}} &= 0.12\% bd \\
 &= 0.12 \times (bd)/100 \\
 &= (0.12 \times 230 \times 575)/100 \\
 &= 158.7 \text{ mm}^2 \approx 160 \text{ mm}^2 \\
 \text{Use 8mm } \Phi \text{ bars} \\
 \text{Spacing} &= ((\pi/4 \times 8^2 \times 1000)/160) \\
 &= 284.65\text{mm} = 280\text{mm c/c}
 \end{aligned}$$

CHECK FOR SHEAR

$$\begin{aligned}
 V_u &= 116.76\text{kN} \\
 T_u &= 116.76 \times 10^3 / (230 \times 575) \\
 &= 0.88\text{N/mm}^2 \\
 p_t &= 100A_{st}/bd \\
 &= (100 \times 934)/(230 \times 575) \\
 &= 0.706\text{N/mm}^2 \\
 Z_c &= 0.545\text{N/mm}^2 \\
 \text{Balanced shear, } V_u - (T_u bd) &= 116.76 - (0.545 \times 230 \times 575) \\
 &= 44.68\text{kN} \\
 S_v > 0.75d &= 0.75 \times 575 \\
 &= 431.25\text{mm}
 \end{aligned}$$

CHECK FOR DEFLECTION

$$\begin{aligned}
 P_t &= 0.706 \\
 (L/d)_{\text{max}} &= (L/d)_{\text{basic}} \times k_t \times k_c \times k_f \\
 &= 20 \times 1.15 \times 1 \times 1 \\
 &= 23 \\
 (L/d)_{\text{actual}} &= (6000/575) \\
 &= 10.43 < 23
 \end{aligned}$$

HENCE SAFE

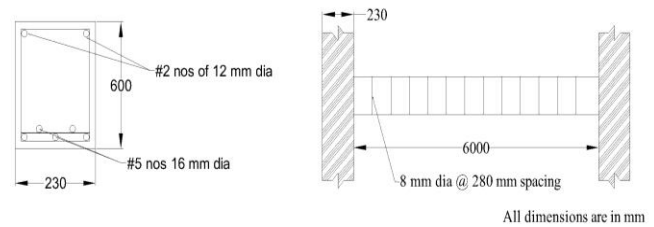


Fig 6: Reinforcement Details of Beam Section

4.4 DESIGN OF COLUMN:

Design of rectangular column:

$$\begin{aligned}
 \text{Column size} &= 0.4 \times 0.5\text{m} \\
 \text{Self-weight of column} &= 0.4 \times 0.5 \times 25 \\
 &= 35\text{kN} \\
 \text{Factored load} &= 1270 + 35 \\
 &= 1305 \\
 \text{Axial load} &= 1305\text{kN} \\
 P &= (0.4 f_{ck} \times A_c) + (0.67 \times f_y \times A_{sc}) \\
 &= 89014.69\text{mm}^2 \\
 \text{Column size} &= 400 \times 500 \\
 &= 200000\text{mm}^2 \\
 A_{sc} &= 0.01 A_g \\
 &= 0.01 \times 89014.69 \\
 &= 890.14\text{mm}^2 \\
 \text{Assume 16mm } \phi \text{ bars} \\
 \text{No of bars} &= 890.14 / (\pi/4 \times 16^2) \\
 &= 4.42 \\
 &= 5 \text{ bars}
 \end{aligned}$$

Slenderness ratio

$$\begin{aligned}
 L_e/d &= 7000/500 \\
 &= 14 > 12
 \end{aligned}$$

Hence it is column.

Eccentricity

$$\begin{aligned}
 E_{\text{max}} &= 1/500 + D/30 \\
 &= 7000/5000 + 500/30 \\
 &= 30.67 \\
 E_{\text{min}} &= 7000/500 + 400/30 \\
 &= 27.34
 \end{aligned}$$

Reinforcement lateral bars

$$\begin{aligned}
 \text{Diameter of lateral} &\leq 1/4 \times \phi \text{ of main bar} \\
 &\leq 1/4 \times 16 \\
 &= 4
 \end{aligned}$$

Assume diameter of the lateral bars = 6mm

Pitch of lateral bars = 16x d
 = 16x6
 = 96mm
 Pitch of lateral bars = 100mm
 Hence safe.

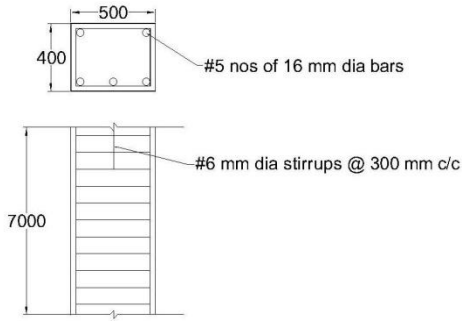


Fig. 6: Reinforcement Details Of Rectangular Column

4.5 DESIGN OF FOUNDATION

DATA

Axial load on column = 1305 kN
 Permissible compressive stress on concrete = 4 N/mm² (M₁₅)

COLUMN BASE:

Area of base plate = $1305/4000 = 0.33 \text{ m}^2$
 Use a square base
 Therefore side of base plate = $\sqrt{0.33} = 0.574 = 600 \text{ mm}$
 Adopt base plate of size 600mm x 600mm
 The projection of the base plate from the edge is obtained as
 a = greater projection = $0.5(600-400) = 100 \text{ mm}$
 b = smaller projection = $0.5(600-500) = 50 \text{ mm}$
 Intensity of the pressure on the plate, = $2050 \times 10^3 / 600 \times 600 = 3.62 \text{ N/mm}^2$
 Permissible bearing stress in the base plate, = 185 N/mm²
 Thickness of base plate, T = $\sqrt{3w / \sigma_{bs}(a^2 - b^2/4)} = \sqrt{3 \times 3.62 / 185(100^2 - 50^2/4)} = 23.46 = 30 \text{ mm}$
 Adopt base plate size = 600mm x 600mm x 30mm

For connecting the column to the base plate, adopt ISA 100x100x10mm angle with 4#, 22mm φ rivets on flange and ISA 75x75x8mm with 3# 22mm φ rivets in the web.

DESIGN OF GUSSETED PLATE

1. Size of the Base Plate

Area of base plate = $1305/4000 = 0.33 \text{ m}^2$
 Adopt ISA 150x150x12 mm angles on flange side with smaller leg horizontal, gusset plate 12mm thick 10mm batten and cover plates = 30mm projection on either sides in direction parallel to web.
 Minimum length required = $(400+20+24+200+60) = 104 \text{ mm}$
 Length of base plate parallel to the flanges = 750mm
 Adopt base plate = 750mm x 750mm

2. Thickness of Base Plate:

Intensity of pressure below the plate = $1305 \times 10^3 / 750 \times 750 = 2.32 \text{ N/mm}^2$
 Cantilever projection of plate from face of the gusset angle = 141mm
 $\mu = wl^2/2 = 2.32 \times 141^2 / 2 = 23062 \text{ Nmm}$
 Thickness of plate required,
 $\mu = \sigma_{bs} bt^2/6$
 $t = \sqrt{6M / \sigma_{bs} b} = \sqrt{6 \times 23062 / 185 \times 1} = 27.35 \text{ mm}$
 In WSD, $\sigma = 0.75 f_y$
 Therefore base plate thickness = 27.35 - 12 = 15.35 mm
 Adopt 750 x 750 x 16mm base plate

Connections

Outstand on each side = $(750 - 400)/2 = 175 \text{ mm}$
 Load on each connection = $(175 \times 750 \times 2.32 / 100) = 304.5 \text{ kN}$
 Using 22mm φ rivets,
 Single shear = $(\pi \times 23.5 \times 100 / 4 \times 1000) = 43.4 \text{ kN}$
 Bearing = $23.5 \times 12 \times 300 / 1000 = 84.6 \text{ kN}$
 Least value = 43.4 kN

$$\text{Number of rivets} = 304.5/43.4 = 7.2 = 8$$

Design of Grillage Foundation

$$\begin{aligned} \text{SBC of the soil} &= 250 \text{ kN/m}^2 \\ \text{Load} &= 1305 \text{ kN} \\ \text{Area of grillage:} \\ \text{Using gusseted base for the column,} \\ \text{Total load} &= (1305 + 10\% \text{ for self weight}) \\ &= 1435.5 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Two-tier girder will be used,} \\ \text{Bottom tier area} &= 1435.5/250 \\ &= 5.74 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Use square grillage} \\ a &= \sqrt{5.74} \\ &= 2.39 \text{ m} = 2.4 \text{ m} \end{aligned}$$

Allow 125mm concrete cover on all sides,
Overall size of block = 2.65x2.65m

Design of Top Tier Girders

$$\begin{aligned} \text{B.M} &= w/8 (l-l_1) \\ W = 1305 \text{ kN, } L = 2.65 \text{ m, } l_1 = 0.75 \text{ m} \\ \text{BM} &= 1305/8(2.65 - 0.75) \\ &= 309.94 \text{ kN} \end{aligned}$$

Allowable stress can be increased by 33.33% since beams are encased in concrete.

$$\begin{aligned} \sigma_{bt} &= (165 \times 1.33) \\ &= 220 \text{ N/mm}^2 \\ Z = \mu/\sigma_{bt} &= 309.94 \times 10^6 / 220 \\ &= 1.409 \times 10^6 \text{ mm}^3 \end{aligned}$$

$$\begin{aligned} \text{Using three beams in top tier,} \\ Z \text{ for each beam} &= 1.409 \times 10^6 / 3 \\ &= 469667 \text{ mm}^3 \end{aligned}$$

Use ISHB 225, with sectional properties
 $Z_{xx} = 487000 \text{ mm}^3$, $t_f = 9.1 \text{ mm}$

$$\begin{aligned} T_w &= 8.6 \text{ mm} \\ \text{Maximum shear force} \\ &= w/2l(l-l_1) \\ &= 1305/2(2.65)(2.65 - 0.75) \\ &= 467.8 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Shear force per beam} \\ &= 467.8/3 \\ &= 156 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Average shear stress } \tau_v \\ &= 156 \times 10^3 / 8.6 \times 225 \\ &= 80.6 \text{ N/mm}^2 < 100 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Minimum gap between two beams} \\ &= 75 \text{ mm} \end{aligned}$$

Design of Bottom Tier Girders

$$\begin{aligned} \text{BM} &= w/8(l-l_2) \\ &= 1305/8(2.65 - 0.75) \\ &= 309.93 \text{ kNm.} \\ Z &= \mu/\sigma_{bt} \end{aligned}$$

$$\begin{aligned} &= 309.93 \times 10^6 / 165 \times 1.33 \\ &= 1.41 \times 10^6 \text{ mm}^4 \end{aligned}$$

$$\begin{aligned} \text{Use 8 beams in bottom tier} \\ Z \text{ for each beam} &= 1.41 \times 10^6 / 8 \\ &= 176.250 \text{ mm}^3 \\ \text{Beam spacing} &= 1/7(2.65 - 0.75) \\ &= 350 \text{ mm} \end{aligned}$$

$$\begin{aligned} \text{Use 8 beams of ISHB 150@ 350mm c/c} \\ \text{Maximum shear force } v \\ &= w/2l(l-l_1) \\ &= 467.83 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Shear force per beam} \\ &= 467.83/8 = 58.5 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Shear stress } \tau_v \\ &= 72.2 \text{ N/mm}^2 < 100 \text{ N/mm}^2 \end{aligned}$$

Adopt separators of angles ISA 50x50x6mm and 2.75m long bolted with 12mm ϕ both to the flanges of the lower tier girders at two ends to prevent girder displacement.

4.6 DESIGN OF STAIRCASE

DOG LEGGED STAIRCASE

$$\begin{aligned} \text{Rise} &= 100 \text{ mm} \\ \text{Thread} &= 400 \text{ mm} \\ \text{Number of steps} &= 15 \\ \text{Width of landing beam} \\ &= 300 \text{ mm} \\ \text{Grade of concrete} &= M_{30} \\ \text{Grade of steel} &= Fe_{415} \end{aligned}$$

To Calculate Effective Span

$$\begin{aligned} \text{Effective span} \\ &= nt + \text{width of the landing beam} \\ &= 15 \times 400 + 300 \\ L &= 6300 \text{ mm} \\ L &= 6.3 \text{ m} \\ \text{Thickness of waist slab} \\ &= \text{span}/20 \\ &= 6300/20 \\ &= 315 \text{ mm} \\ &= 0.315 \text{ m} \\ \text{Effective depth} &= 0.315 - 0.025 \\ &= 0.29 \text{ m} \end{aligned}$$

Loads

$$\begin{aligned} \text{Dead load slab on step } (w_s) \\ &= 1 \times 0.315 \times 25 \\ &= 7.875 \text{ m}^2 \\ \text{Dead load of step of horizontal span} \\ &= (w_s \times \sqrt{R^2 + T^2}) / T \\ W &= (7.875 \times \sqrt{0.1^2 + 0.4^2}) / 0.4 \end{aligned}$$

$$\begin{aligned}
 &= 8.11\text{m} \\
 \text{Dead load on step (D}_o\text{)} &= 0.5 \times R \times T \times 25 \\
 &= 0.5 \times 0.1 \times 0.4 \times 25 \\
 \text{(D}_o\text{)} &= 0.5 \text{ kN/m} \\
 \text{Load step per m length} &= D_o \times 1000 / T \\
 &= 0.5 \times 1 / 0.4 \\
 &= 1.25 \text{ kN/m}^2 \\
 \text{Total service load} &= D.L + L.L + F.L \\
 \text{Live load for residential building} &= 2 \text{ to } 3 \text{ kN/m}^2 \\
 \text{Live load for public building} &= 5 \text{ kN/m}^2 \\
 \text{Weight of floor load} &= 0.6 \text{ kN/m}^2 \\
 \text{Dead load} &= 8.11 + 1.25 \\
 &= 9.36 \text{ kN/m}^2 \\
 W &= 9.36 + 5 + 0.6 \\
 &= 14.96 \text{ kN/m}^2 \\
 \text{Factored load (w}_u\text{)} &= 1.5 \times w \\
 &= 1.5 \times 14.96 \\
 &= 22.44 \text{ kN/m}^2
 \end{aligned}$$

BENDING MOMENT

$$\begin{aligned}
 \text{Bending moment at the center of span (m}_u\text{)} &= w l^2 / 8 \\
 &= 22.44 \times 4^2 / 8 \\
 &= 51.86 \text{ kNm}
 \end{aligned}$$

CHECK FOR DEPTH OF WAIST SLAB

$$\begin{aligned}
 D &= \sqrt{(m_u / 0.138 f_{ck} b)} \\
 &= \sqrt{(51.86 \times 10^6 / 0.138 \times 30 \times 1000)} \\
 D &= 111.92 \\
 D &= 112 < 315 \text{ mm.}
 \end{aligned}$$

MAIN REINFORCEMENT

$$\begin{aligned}
 M_u &= 0.87 f_y a_{st} d (1 - a_{st} f_y / f_{ck} b d) \\
 A_{st} &= 513.62 \text{ mm}^2 \\
 \text{Use } 12\text{mm } \phi \text{ bars} & \\
 \text{Spacing} &= a_{st} (\text{provided}) / a_{st} (\text{required}) \\
 &= ((\pi / 4 \times 12^2) / 513.62) \times 1000 \\
 &= 220 \text{ mm c/c}
 \end{aligned}$$

Provide 12mm ϕ bars @ 220mm c/c as main reinforcement
Hence safe.

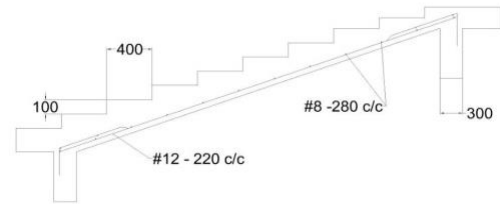


Fig. 7: Reinforcement Details of Staircase

5. CONCLUSION

Thus we designed the well facilitated auditorium with a suitable steel grillage foundation. These designs are carried out with the guidance of IS 456:2000. A proper fittings and grouting has to be provided to the grillage. The steel grillage is provided with respective corrosive resistant coatings to ensure the risk of disturbing contaminants.

The planning of auditorium was done as per guidelines. The designs of various structural elements were done by limit state method. The project portrays all the fundamental design and load consideration in the erection of the building. All design in accordance with those specified in Bureau of Indian Standard and IS 456:2000. Finally the auditorium was designed with a steel grillage foundation to meet the necessary requirements.

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